



# MICRO DATA AND MACRO TECHNOLOGY

GROUP 10

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## **Department of Economics**

- Princeton University

## **Main Academic Positions**

- Assistant Professor of Economics, Princeton University, 2013 - present
- Economist, Federal Reserve Bank of Chicago, 2010 - 2013



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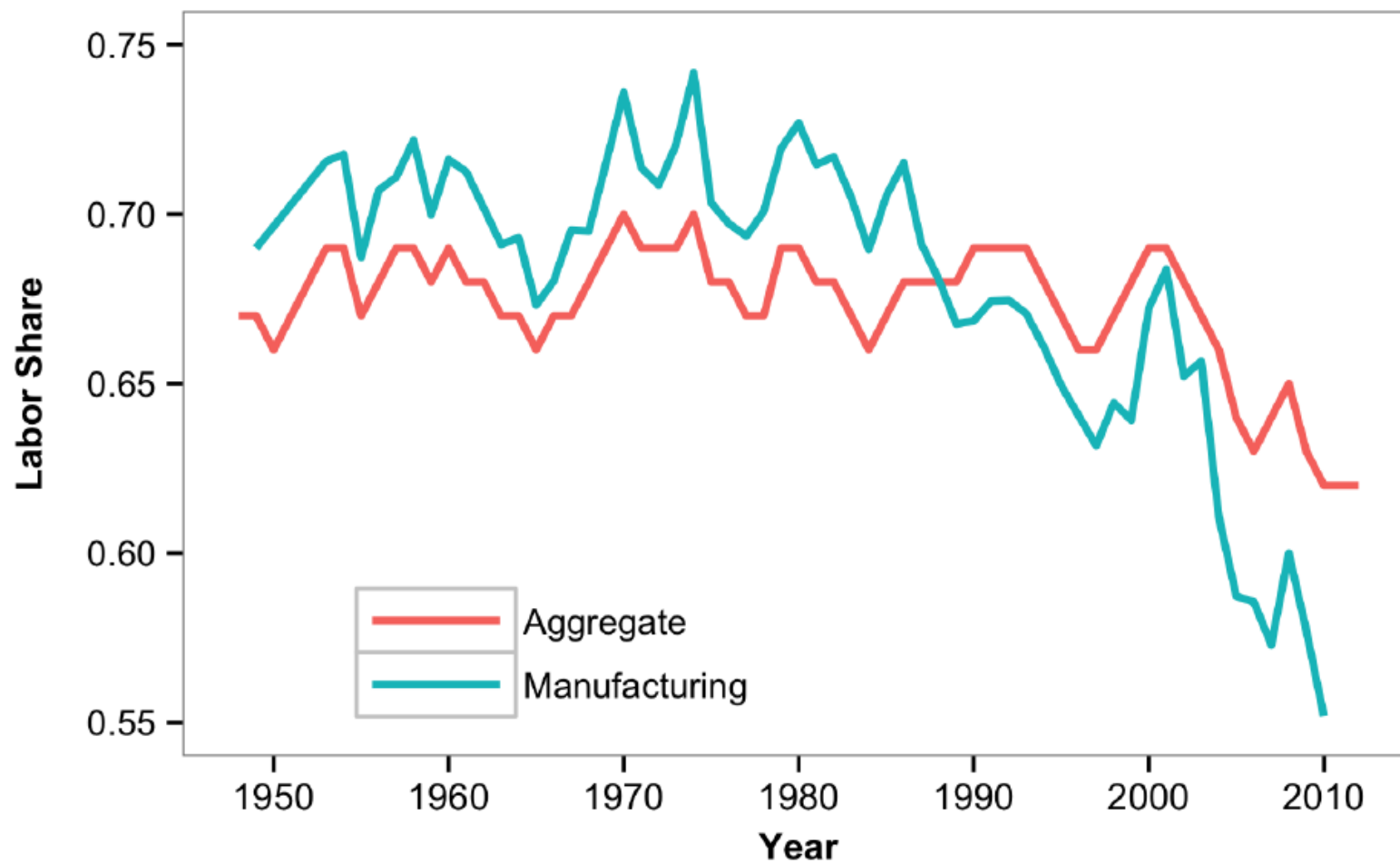
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### **Main Academic Directions**

- Areas of specialization Industrial Organization; Productivity; Applied Econometrics.



# LABOR'S SHARE HAS FALLEN





# WHY HAS THE LABOR SHARE FALLEN?

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## Supply

- Piketty: Increased capital accumulation
- Karabarbounis & Neiman: Investment-specific technical change

## Demand

- Automation / Offshoring

**Key is the Aggregate Elasticity of Substitution:**

$$\sigma^{\text{agg}} \equiv \frac{d \ln K/L}{d \ln w/r}$$



# AGGREGATE CAPITAL-LABOR ELASTICITY OF SUBSTITUTION

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Impossibility Theorem of Diamond, McFadden, & Rodriguez (1978)

Cannot identify  $\sigma$  or bias of tech. with time series of quantities and prices  
Need variation in prices that is independent of technology

Parametric assumptions on the bias of technical change

No bias/constant bias



## METHOD 2: USE MICRO DATA

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### More plausibly exogenous differences in prices

Houthakker (1955) micro and macro elasticities can be very different  
an economy of Leontief micro units can have a Cobb–  
Douglas aggregate production function.

Typical estimate: 0.4-0.5

Identifies a micro elasticity of substitution



## 2.1 SIMPLE EXAMPLE

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$$Y_i = \left[ (A_i K_i)^{\frac{\sigma-1}{\sigma}} + (B_i L_i)^{\frac{\sigma-1}{\sigma}} \right]^{\frac{\sigma}{\sigma-1}}$$

$$\sigma^{\text{agg}} \equiv \frac{d \ln K/L}{d \ln w/r}$$

$$K \equiv \sum_{i \in I} K_i \quad L \equiv \sum_{i \in I} L_i$$

- a large set of plants  $I$
- constant elasticity of substitution  $\sigma$
- CES production function
- Capital  $K_i$  labor  $L_i$
- Capital-augmenting productivity  $A_i$
- Labor-augmenting productivity  $B_i$





## 2.1 SIMPLE EXAMPLE

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$$\alpha_i \equiv \frac{rK_i}{rK_i + wL_i} \quad \alpha \equiv \frac{rK}{rK + wL} \quad \alpha = \sum_{i \in I} \alpha_i \theta_i \quad \theta_i \equiv \frac{rK_i + wL_i}{rK + wL}$$

$$\sigma - 1 = \frac{d \ln rK_i / wL_i}{d \ln w/r} = \frac{d \ln \alpha_i / (1 - \alpha_i)}{d \ln w/r} = \frac{1}{\alpha_i(1 - \alpha_i)} \frac{d \alpha_i}{d \ln w/r}$$

$$\sigma^{\text{agg}} - 1 = \frac{d \ln rK / wL}{d \ln w/r} = \frac{d \ln \alpha / (1 - \alpha)}{d \ln w/r} = \frac{1}{\alpha(1 - \alpha)} \frac{d \alpha}{d \ln w/r}$$

$$\sigma^{\text{agg}} - 1 = \frac{1}{\alpha(1 - \alpha)} \sum_{i \in I} \alpha_i(1 - \alpha_i)(\sigma - 1)\theta_i + \frac{1}{\alpha(1 - \alpha)} \sum_{i \in I} \alpha_i \theta_i \frac{d \ln \theta_i}{d \ln w/r}$$




## 2.1 SIMPLE EXAMPLE

- Dixit–Stiglitz preference
- monopolistically competitive
- common elasticity of demand  $\varepsilon > 1$

$$h_i(\mathbf{p}, u) = \frac{\partial e(\mathbf{p}, u)}{\partial p_i}$$

$$\left( \sum_{i \in I} D_i^{\frac{1}{\varepsilon}} Y_i^{\frac{\varepsilon-1}{\varepsilon}} \right)^{\frac{\varepsilon}{\varepsilon-1}}$$


$$\frac{d \ln \theta_i}{d \ln w/r} = (\varepsilon - 1)(\alpha_i - \alpha)$$



## 2.1 SIMPLE EXAMPLE

$$\sigma^{\text{agg}} = (1 - \chi)\sigma + \chi\varepsilon$$

aggregate  
EoS

plant level  
EoS

plant level  
elasticity of  
demand



$\sigma$ : substitution **within** plants

$\sigma^{\text{agg}}$ : substitution **across** plants

$\varepsilon$ : **heterogeneity** in capital intensity

$\mathbf{X}$ : proportional to variance of capital shares

$$\chi \equiv \sum_{i \in I} \frac{(\alpha_i - \alpha)^2}{\alpha(1 - \alpha)} \theta_i$$



## 2.2 BASELINE MODEL

$$F_{ni}(K_{ni}, L_{ni}, M_{ni}) = \left( \left[ (A_{ni}K_{ni})^{\frac{\sigma_n-1}{\sigma_n}} + (B_{ni}L_{ni})^{\frac{\sigma_n-1}{\sigma_n}} \right]^{\frac{\sigma_n-1}{\sigma_n-1} \frac{n-1}{\zeta_n}} + (C_{ni}M_{ni})^{\frac{\zeta_n-1}{\zeta_n}} \right)^{\frac{\zeta_n}{Ln-1}}$$

$$Y \equiv \left[ \sum_{n \in N} D_n^{\frac{1}{\eta}} Y_n^{\frac{\eta-1}{\eta}} \right]^{\frac{\eta}{\eta-1}} \quad Y_n \equiv \left( \sum_{i \in I_n} D_{ni}^{\frac{1}{\varepsilon_n}} Y_{ni}^{\frac{\varepsilon_n-1}{\varepsilon_n}} \right)^{\frac{\varepsilon_n}{\varepsilon_n-1}}$$

$$Y_{ni} = F_{ni}(K_{ni}, L_{ni}, M_{ni})$$

$$\max_{P_{ni}, Y_{ni}, K_{ni}, L_{ni}, M_{ni}} P_{ni} Y_{ni} - r K_{ni} - w L_{ni} - q M_{ni}$$

- Plant i in industry n produces with the production function
- elasticity of substitution between capital and labor :  $\sigma_n$
- elasticity of substitution between materials and its capital-labor bundle :  $\zeta_n$
- Each plant in industry n faces a demand curve with constant elasticity  $\varepsilon_n$
- q : price of materials, each plant maximizes profit
- subject to the technological constraint



## 2.2 BASELINE MODEL

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Demand curve

$$Y_{ni} = Y_n (P_{ni}/P_n)^{-\varepsilon_n}$$

Price index for industry n

$$P_n \equiv \left( \sum_{i \in I_n} D_{ni} P_{ni}^{1-\varepsilon_n} \right)^{\frac{1}{1-\varepsilon_n}}$$

$$\sigma_n^N \equiv \frac{d \ln K_n / L_n}{d \ln w / r}$$

$$\alpha_{ni} = \frac{rK_{ni}}{rK_{ni} + wL_{ni}}$$

$$\theta_{ni} = \frac{rK_{ni} + wL_{ni}}{rK_n + wL_n}$$

$$s_{ni}^M \equiv \frac{qM_{ni}}{rK_{ni} + wL_{ni} + qM_{ni}}$$



## 2.3 PROPOSITIONS: 1 & 2

**PROPOSITION 1:** Under Assumption 1, the industry elasticity of substitution is

$$\sigma_n^N = (1 - \chi_n)\sigma_n + \chi_n \left[ (1 - \bar{s}_n^M)\varepsilon_n + \bar{s}_n^M \zeta_n \right]$$

$$\chi_n = \sum_{i \in I_n} \frac{(\alpha_{ni} - \alpha_n)^2}{\alpha_n(1 - \alpha_n)} \theta_{ni} \quad \bar{s}_n^M = \frac{\sum_{i \in I_n} (\alpha_{ni} - \alpha_n)(\alpha_{ni} - \alpha^M) \theta_{ni} s_{ni}^M}{\sum_{i \in I_n} (\alpha_{ni} - \alpha_n)(\alpha_{ni} - \alpha^M) \theta_{ni}}$$

**PROPOSITION 2:** The aggregate elasticity between capital and labor

$$\sigma^{\text{agg}} = (1 - \chi^{\text{agg}})\bar{\sigma}^N + \chi^{\text{agg}} \left[ (1 - \bar{s}^M)\eta + \bar{s}^M \bar{\zeta}^N \right]$$

$$\chi^{\text{agg}} \equiv \sum_{n \in N} \frac{(\alpha_n - \alpha)^2}{\alpha(1 - \alpha)} \theta_n$$

$$\bar{s}^M \equiv \sum_{n \in N} \frac{(\alpha_n - \alpha)(\alpha_n - \alpha^M) \theta_n}{\sum_{n' \in N} (\alpha_{n'} - \alpha)(\alpha_{n'} - \alpha^M) \theta_{n'}} s_n^M$$

$$\bar{\sigma}^N \equiv \sum_{n \in N} \frac{\alpha_n(1 - \alpha_n) \theta_n}{\sum_{n' \in N} \alpha_{n'}(1 - \alpha_{n'}) \theta_{n'}} \sigma_n^N$$

$$\bar{\zeta}^N \equiv \sum_{n \in N} \frac{(\alpha_n - \alpha)(\alpha_n - \alpha^M) \theta_n s_n^M}{\sum_{n' \in N} (\alpha_{n'} - \alpha)(\alpha_{n'} - \alpha^M) \theta_{n'} s_{n'}^M} \zeta_n^N$$



## BEFORE EMPIRICAL

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Two Propositions throughout the whole article

$$\sigma_n^N = (1 - \chi_n)\sigma_n + \chi_n[(1 - \bar{s}_n^M)\varepsilon_n + \bar{s}_n^M\zeta_n]$$

$$\sigma^{agg} = (1 - \chi^{agg})\bar{\sigma}^N + \chi^{agg}[(1 - \bar{s}^M)\eta + \bar{s}^M\bar{\zeta}^N]$$

Elasticity: substitution elasticity, demand elasticity

Heterogeneity: capital intensive heterogeneity, intermediate production heterogeneity



# BEFORE EMPIRICAL

Two Propositions throughout the whole article

$$\sigma_n^N = (1 - \chi_n) \sigma_n + \chi_n [(1 - \bar{s}_n^M) \varepsilon_n + \bar{s}_n^M \zeta_n]$$

Elasticity

substitution elasticity

demand elasticity

Heterogeneity

capital intensive heterogeneity

intermediate production heterogeneity

$$\sigma^{agg} = (1 - \chi^{agg}) \bar{\sigma}^N + \chi^{agg} [(1 - \bar{s}^M) \eta + \bar{s}^M \bar{\zeta}^N]$$





# DATA - MICRO DATA ON MANUFACTURING PLANTS

## The U.S. Census of Manufactures

every 5 years, 1987 to 2007

### **Capital costs**

Perpetual inventory

Total stock of structures

Equipment capitals

External real rental rate of return: Harper,  
Berndt, Wood (1989)

### **Labor costs**

Total salaries and wages at the plant level

## Annual Survey of Manufactures (ASM)

1977 to 2007

### **Capital Statistics**

Additionally include machinery rents

### **Labor costs**

Additionally include supplemental labor  
costs

Benefits

Payrolls

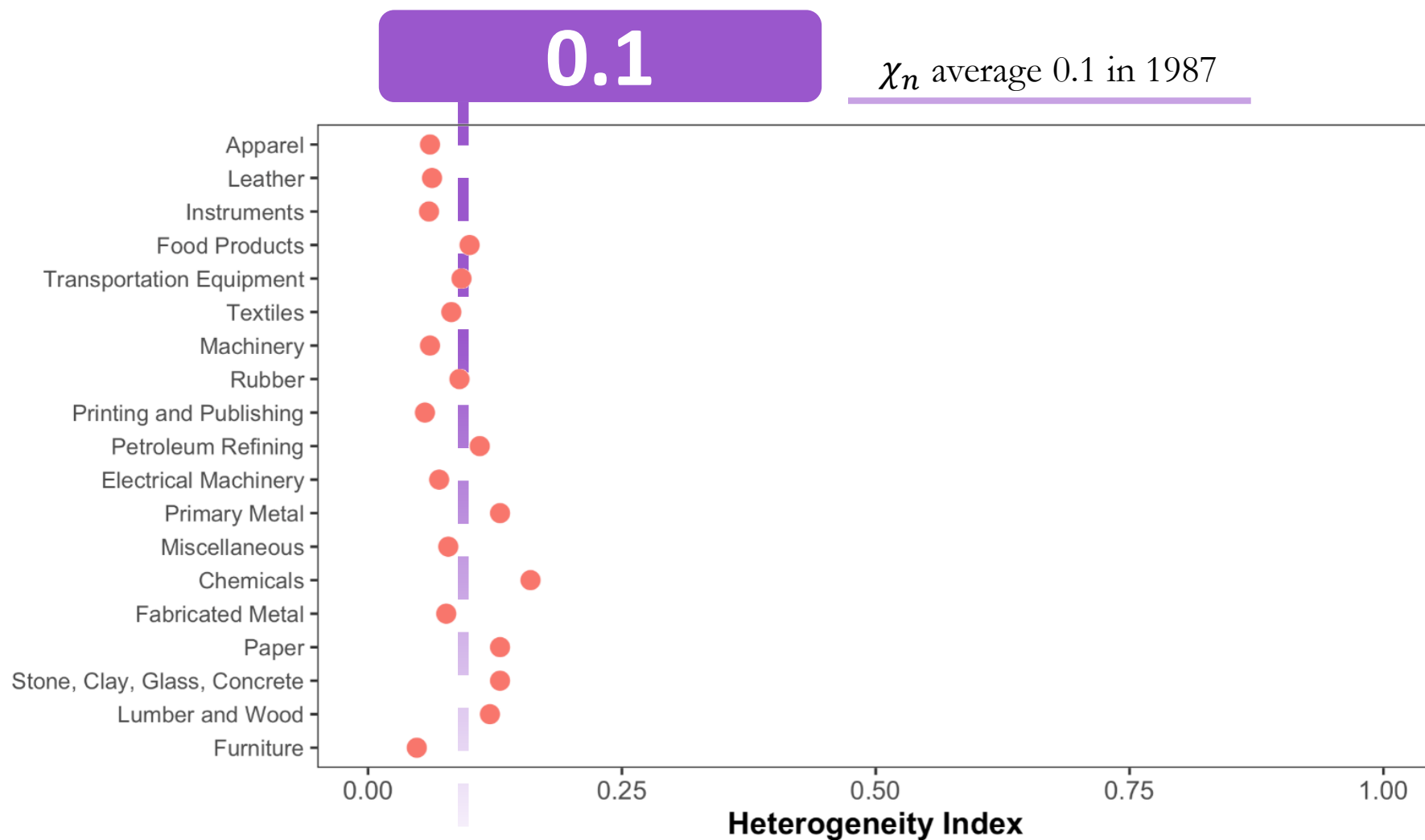
Taxes

**Industry definition: Changes from SIC to NAICS in 1997**



## 3.2 MICRO HETEROGENEITY

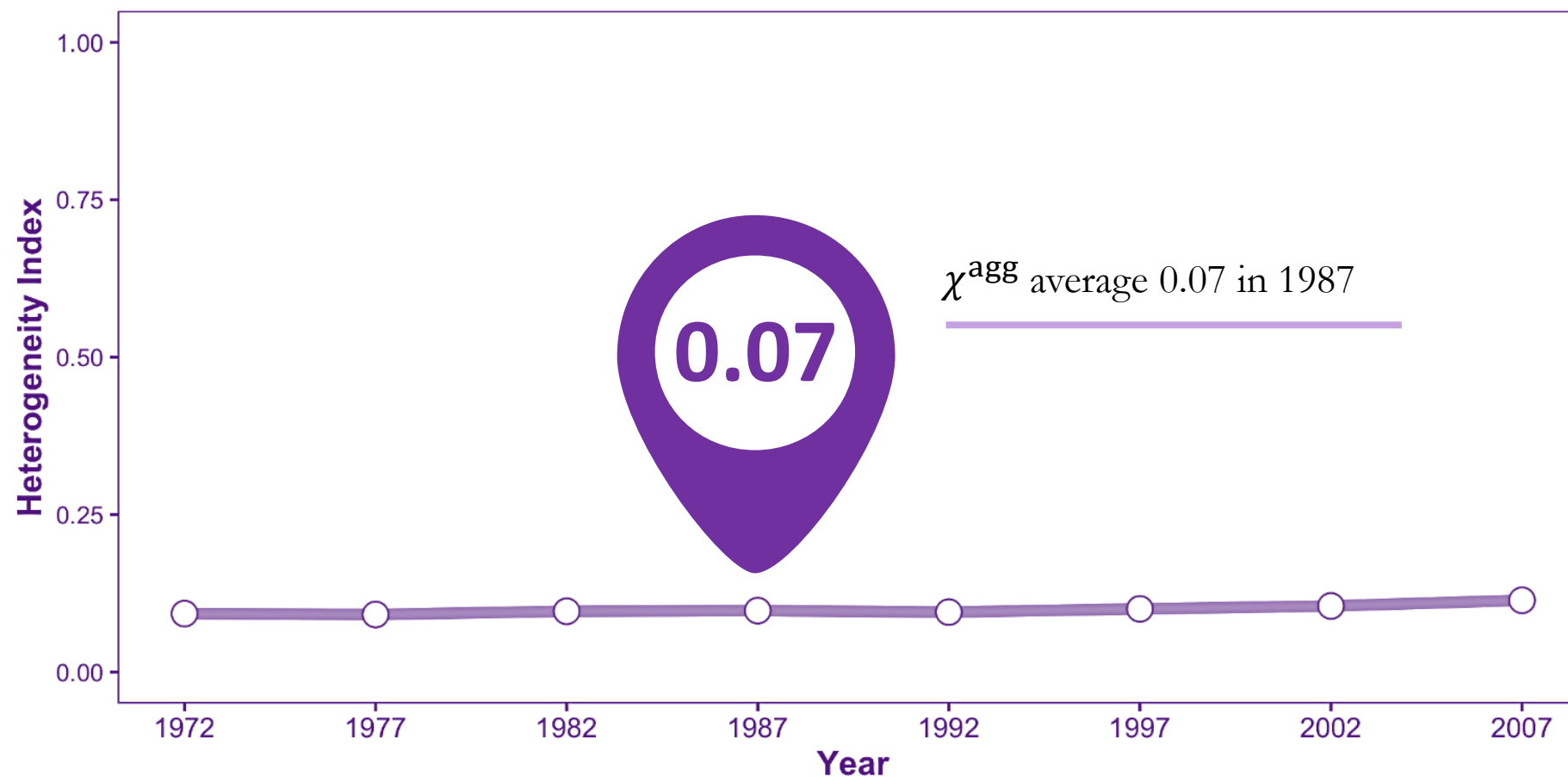
$$\sigma_n^N = (1 - \chi_n)\sigma_n + \chi_n[(1 - \bar{s}_n^M)\varepsilon_n + \bar{s}_n^M\zeta_n]$$





## 3.2 MICRO HETEROGENEITY

$$\sigma_n^N = (1 - \chi_n)\sigma_n + \chi_n[(1 - \bar{s}_n^M)\varepsilon_n + \bar{s}_n^M\zeta_n]$$





### 3.3 PLANT-LEVEL ELASTICITY OF SUBSTITUTION

Regression model

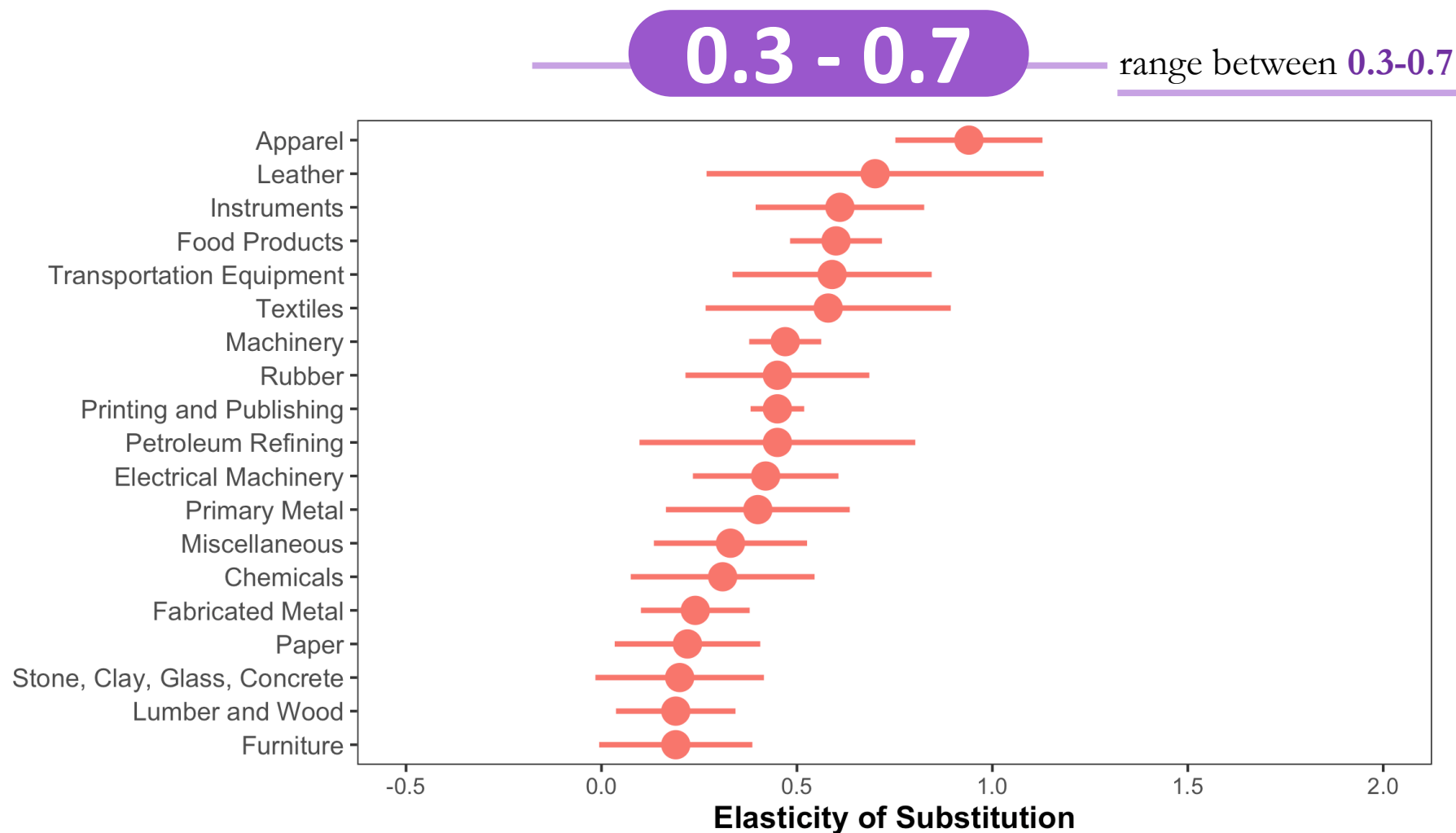
$$\log \frac{rK_{nic}}{wL_{nic}} = \beta_n \log w_c + \gamma_n X_{nic} + \epsilon_{nic}$$

$$\beta_n = \frac{d \log \frac{rK_{nic}}{wL_{nic}}}{d \log \frac{w_c}{r_c}} = \sigma_n - 1$$

- Cross-sectional data
- Same cost of capital
- Residual wage

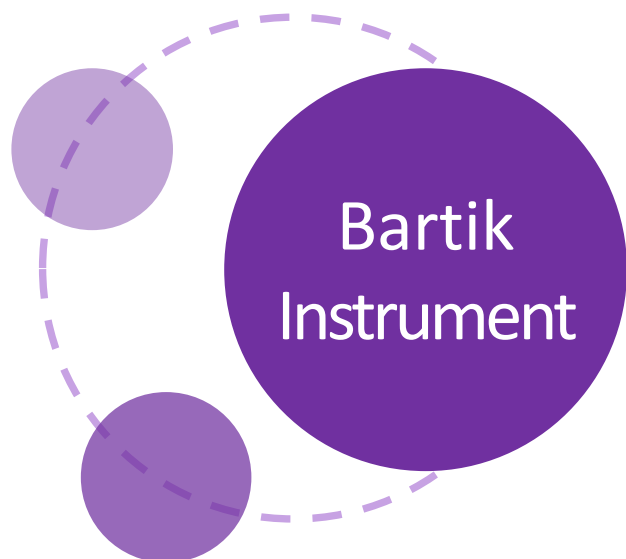


## 3.3 PLANT-LEVEL ELASTICITY OF SUBSTITUTION





## 3.3.1 IV



Heterogeneity of industrial composition

Industry expanding  
in employment



labor demand

→  $w_c$



$$g_n(t) = \frac{1}{10} \ln\left(\frac{L_n(t)}{L_n(t-10)}\right)$$
$$Z_j(t) = \sum_{n \in N^S} \omega_{j,n}(t-10) g_n(t)$$

$$\frac{d(\text{Labor demand})}{d(\text{Local expanding in employment})}$$



## 3.3.1 IV



Heterogeneity of industrial composition

Industry wage premium

labor supply

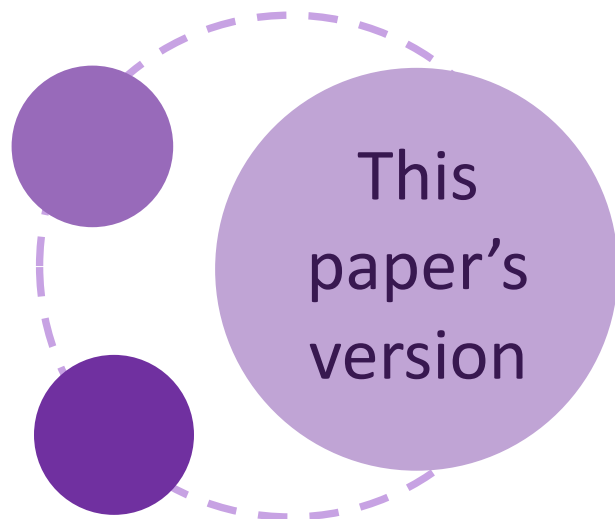
$w_c$

$$\sum_{n \in N^S} \hat{\omega}_{j,n}(t) [v_n(t) - v_n(t-10)]$$
$$\sum_{n \in N^S} v_n(t) [\hat{\omega}_{j,n}(t) - \omega_{j,n}(t-10)]$$

$$\frac{d(\text{Labor supply})}{d(\text{Local wage premium})}$$



## 3.3.1 IV



Short-coming of previous IV: Ignorant of input-output linkages

Better Amenities  $\longrightarrow$  lower wage

IV: Measures of local amenities based on climate and geography





### 3.3.1 IV

$$\sigma_n^N = (1 - \chi_n)\sigma_n + \chi_n[(1 - \bar{s}_n^M)\varepsilon_n + \bar{s}_n^M\zeta_n]$$

#### IV ESTIMATES OF THE PLANT CAPITAL-LABOR SUBSTITUTION ELASTICITY

Year	OLS		Bartik	BGS	Amenities		All
1987	0.44(0.04)	0.54(0.03)	0.52(0.04)	0.45(0.09)	0.45(0.07)	0.48(0.06)	0.51(0.04)
1992	0.47(0.03)	0.52(0.03)	0.45(0.04)	0.48(0.04)	0.57(0.06)	0.55(0.05)	0.50(0.03)
1997	0.29(0.05)	0.48(0.04)	0.41(0.11)	0.36(0.08)	0.28(0.09)	0.40(0.07)	0.41(0.05)
2002	0.31(0.06)	0.48(0.05)	0.31(0.10)	0.37(0.06)	0.33(0.13)	0.42(0.11)	0.42(0.06)
2007	0.45(0.04)	0.58(0.03)	0.51(0.05)	0.56(0.05)	0.49(0.09)	0.53(0.07)	0.54(0.04)
Wage	Pop Census	LBD	LBD	LBD	Pop Census	LBD	LBD





## 3.3.2 OTHER THREATS TO IDENTIFICATION

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### Rental rate



Reflect wage



Difference in creditworthiness

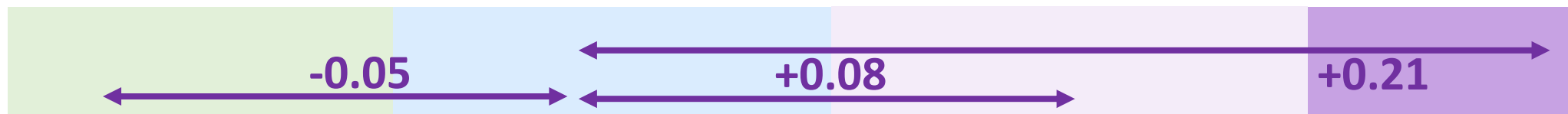


Different capital taxes and subsidies

### 3.3.2 OTHER THREATS TO IDENTIFICATION

ROBUSTNESS CHECKS FOR PLANT CAPITAL-LABOR SUBSTITUTION ELASTICITY

	(1)	(2)	(3)	(4)	(5)	(6)	(7)
	Separate OLS	Singe OLS ( <b>Baseline</b> )	Equipment Capital	Firm FE	State FE	ASM Only	Book Value Capital
1987	0.43	0.44(0.04)	0.45(0.03)	0.57(0.07)	0.39(0.04)	0.40(0.08)	0.42(0.04)
1992	0.48	0.47(0.03)	0.47(0.03)	0.65(0.06)	0.31(0.03)	0.67(0.07)	0.39(0.03)
1997	0.34	0.29(0.05)		0.66(0.06)	0.32(0.05)	0.42(0.09)	0.27(0.05)
2002	0.34	0.31(0.06)		0.59(0.06)	0.41(0.07)	0.52(0.09)	0.22(0.07)
2007	0.38	0.45(0.04)		0.55(0.07)	0.48(0.05)	0.37(0.07)	0.39(0.04)



- Firm-wide wage setting procedures compress wage differences within firms
- Measure error in plant-level capital stock



## 3.4 AGGREGATION

$$\sigma_n^N = (1 - \chi_n)\sigma_n + \chi_n[(1 - \bar{s}_n^M)\varepsilon_n + \bar{s}_n^M\zeta_n]$$

$\zeta_n$

Plant elasticity of substitution between materials and non-materials input

### Same regression model

$$\begin{aligned} &\log \frac{rK_{nic} + wL_{nic}}{qM_{nic}} \\ &= (1 - \zeta)(1 - \alpha_{nic}) \log w_c \\ &\quad + \gamma_n X_{nic} + \epsilon_{nic} \end{aligned}$$

### PLANT-LEVEL ELASTICITIES OF SUBSTITUTION

1987	1.03(0.12)
1992	0.83(0.10)
1997	0.69(0.07)
2002	0.78(0.08)
2007	0.57(0.06)



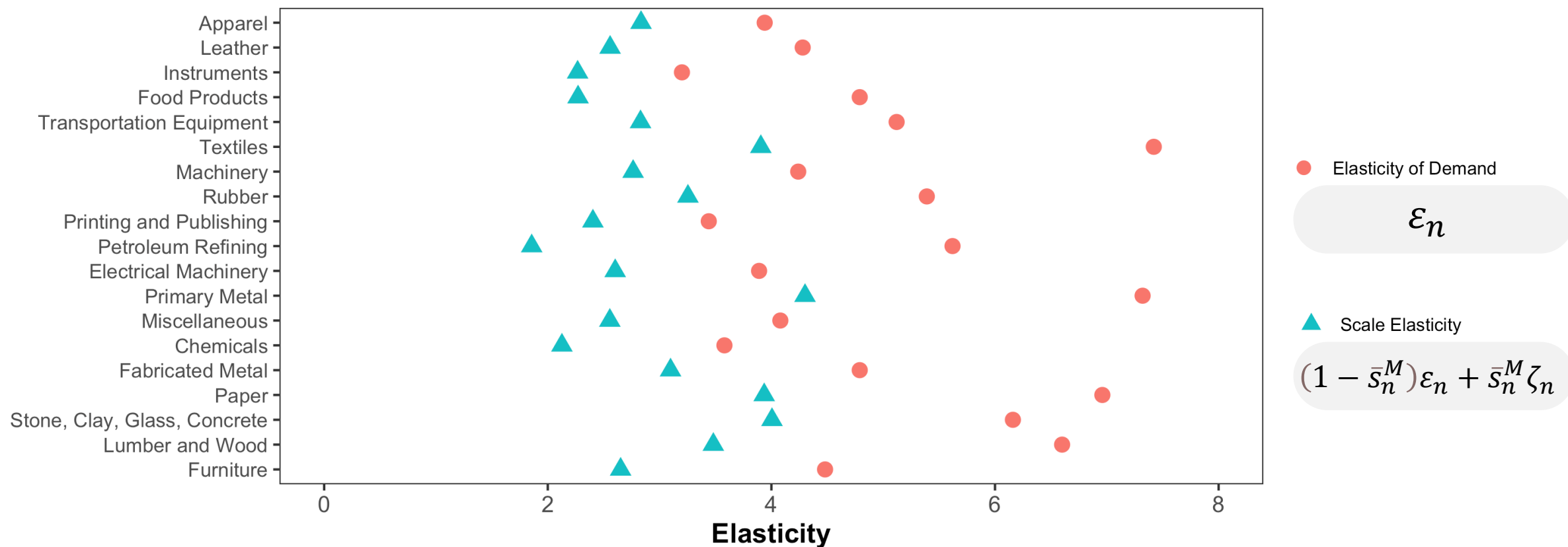
## 3.4 AGGREGATION

$$\sigma_n^N = (1 - \chi_n)\sigma_n + \chi_n[(1 - \bar{s}_n^M)\varepsilon_n + \bar{s}_n^M\zeta_n]$$

$\varepsilon_n$

Optimal price setting behavior: Profit maximization

$$\frac{\varepsilon}{\varepsilon - 1} = \frac{P}{MC}$$



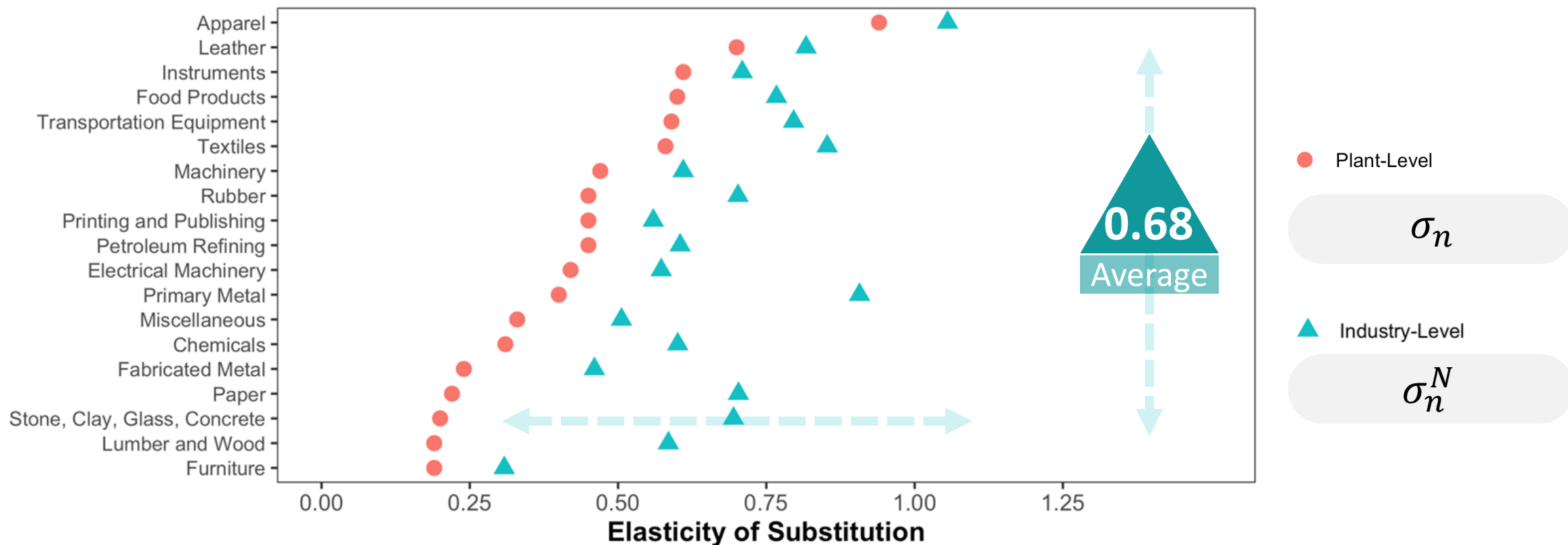


## 3.4 AGGREGATION

$$\sigma_n^N = (1 - \chi_n)\sigma_n + \chi_n[(1 - \bar{s}_n^M)\varepsilon_n + \bar{s}_n^M\zeta_n]$$

$\sigma_n^N$

### Aggregation of industrial elasticity of substitution





# 3.4 AGGREGATION

$$\sigma^{\text{agg}} = (1 - \chi^{\text{agg}})\bar{\sigma}^N + \chi^{\text{agg}}[(1 - \bar{s}^M)\eta + \bar{s}^M\bar{\zeta}^N]$$



$$\log q_{n,t} = -\eta \log p_{n,t} + \alpha_n + \beta_t + \text{Controls} + \varepsilon_n$$



IV: Avg cost as supply shifter



Results:  $\eta$  around 1, set to 1

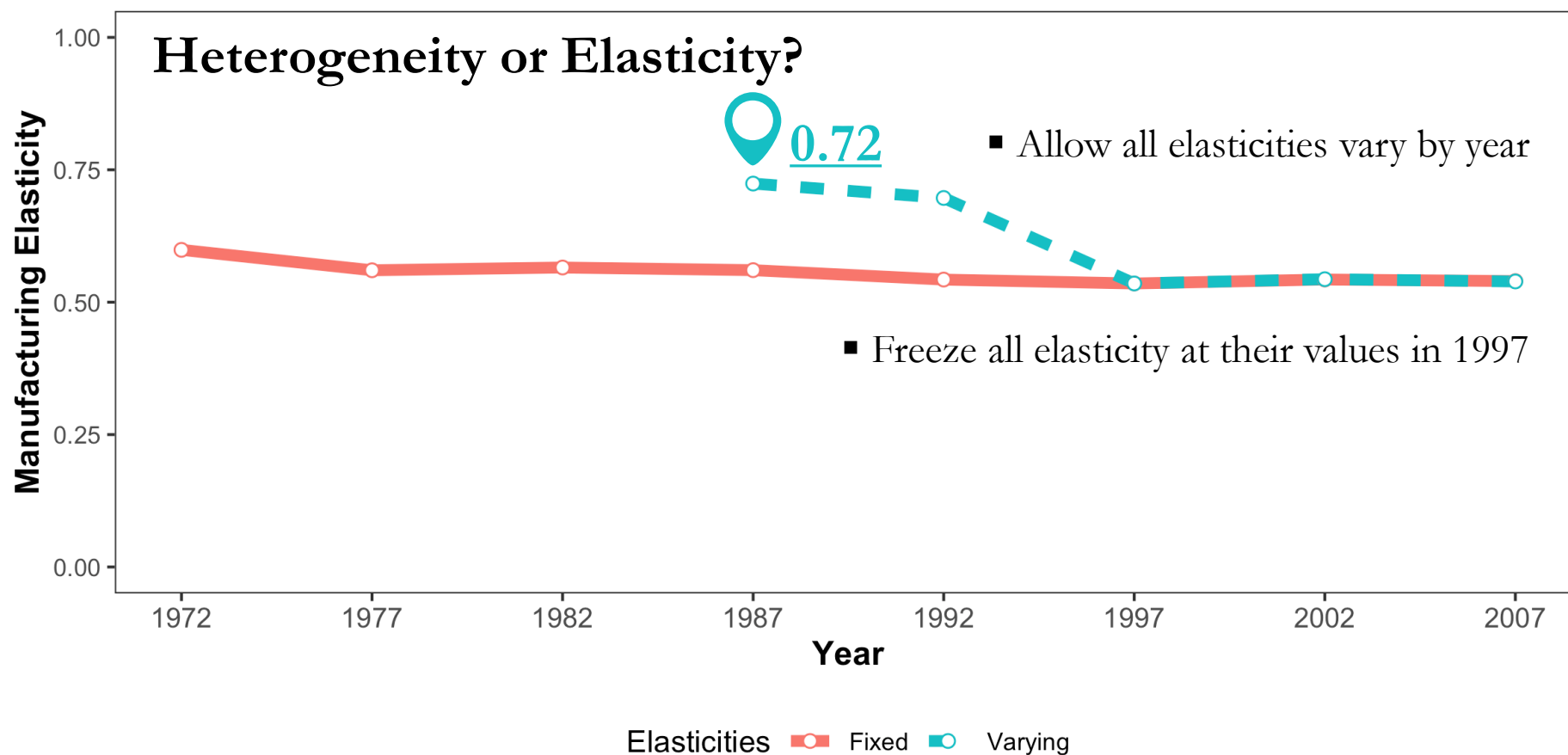
Industry Definition					
Instrument	4-Digit			2-Digit	
None	0.87(0.02)	0.87(0.02)	0.46(0.03)	0.97(0.05)	-0.07(0.04)
APL	1.23(0.01)	1.28(0.01)	2.67(0.05)	1.14(0.04)	1.85(0.34)
Avg Cost	1.17(0.01)	1.13(0.01)	1.89(0.03)	1.16(0.04)	0.65(0.09)
Industry-Year Controls	None	3-Digit FE	6-Digit Trends	None	3-Digit Trends

## 3.4 AGGREGATION

$$\sigma^{\text{agg}} = (1 - \chi^{\text{agg}})\bar{\sigma}^N + \chi^{\text{agg}}[(1 - \bar{s}^M)\eta + \bar{s}^M\bar{\zeta}^N]$$

$\sigma^{\text{agg}}$

### Manufacturing sector-level elasticity of substitution



$\varepsilon_n$

5.0 → 3.3

$\sigma_n$

0.48 → 0.34





## 4 ADDITIONAL MARGINS OF ADJUSTMENT

Entry and Exit

$$\sigma^{\text{agg}} = (1 - \chi) \left[ \sigma + \frac{\int (\alpha_\tau - \alpha) \frac{dE_\tau}{d \ln w/r} \theta_\tau dT(\tau)}{\int \alpha_\tau (1 - \alpha_\tau) \theta_\tau dT(\tau)} \right] + \chi[(1 - \bar{s}^M) \varepsilon + \bar{s}^M \bar{\zeta}^N]$$

Upper bound: Baseline Model

$$\frac{\varepsilon}{\varepsilon - 1} \frac{\text{Variable Costs}}{\text{Variable Costs} + \text{Overhead Costs}} = \frac{\hat{\varepsilon}}{\hat{\varepsilon} - 1}$$

Lower bound: Long-run elasticity =  $\frac{\beta}{1 - \rho_5 - \rho_{10}}$

$$\log \frac{K_{itc}}{L_{itc}} = \rho_5 \log \frac{K_{itc}}{L_{itc}} + \rho_{10} \log \frac{K_{itc}}{L_{itc}} + \beta \log \frac{w_{tc}}{r_t} + \eta_i + \delta_t + \epsilon_{nic}$$



## 4 ADDITIONAL MARGINS OF ADJUSTMENT

Entry and Exit

$$\sigma^{\text{agg}} = (1 - \chi) \left[ \sigma + \frac{\int (\alpha_\tau - \alpha) \frac{dE_\tau}{d \ln w/r} \theta_\tau dT(\tau)}{\int \alpha_\tau (1 - \alpha_\tau) \theta_\tau dT(\tau)} \right] + \chi [(1 - \bar{s}^M) \varepsilon + \bar{s}^M \bar{\zeta}^N]$$

Upper bound: Baseline Model

$$\frac{\varepsilon}{\varepsilon - 1} \frac{\text{Variable Costs}}{\text{Variable Costs} + \text{Overhead Costs}} = \frac{\hat{\varepsilon}}{\hat{\varepsilon} - 1}$$

Interval [0.35, 0.65]

0.35 - 0.65

Lower bound: Long-run elasticity =  $\frac{\beta}{1 - \rho_5 - \rho_{10}}$

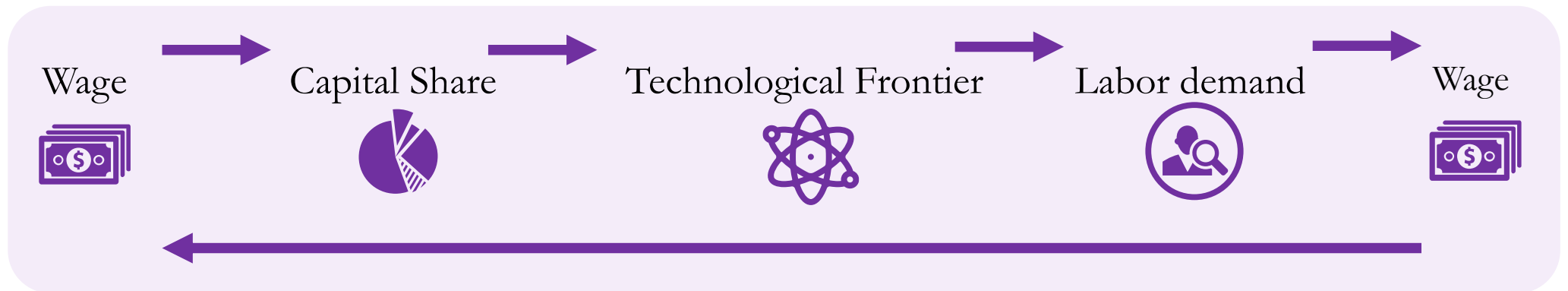
$$\log \frac{K_{itc}}{L_{itc}} = \rho_5 \log \frac{K_{itc}}{L_{itc}} + \rho_{10} \log \frac{K_{itc}}{L_{itc}} + \beta \log \frac{w_{tc}}{r_t} + \eta_i + \delta_t + \epsilon_{nic}$$



## 4 ADDITIONAL MARGINS OF ADJUSTMENT

- **Adjustment and Friction**
  - | Adjustment cost
  - | Misallocation frictions

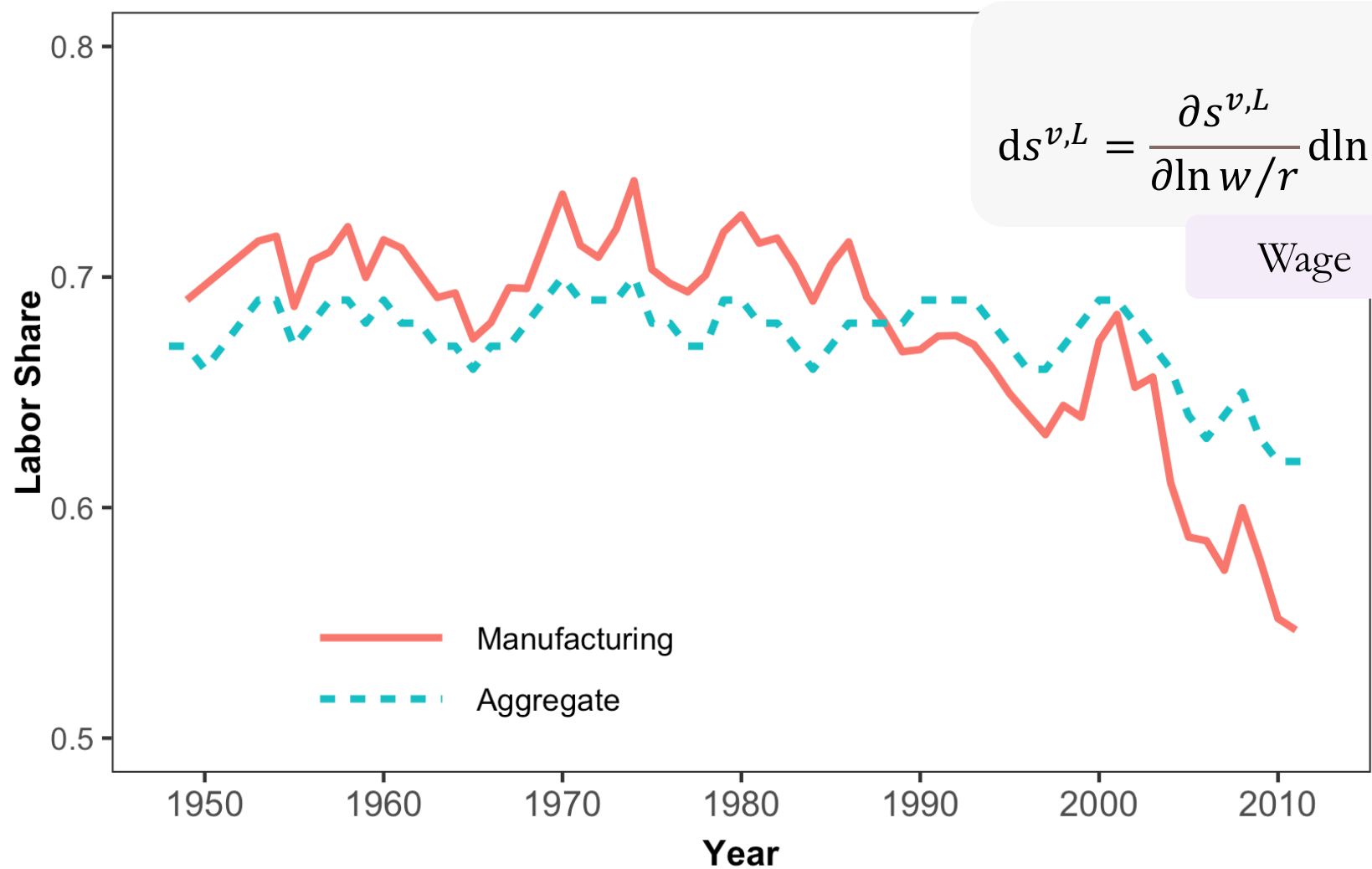
- **Shifts in the technological frontier**



- **Other considerations**
  - | Intangible capital
  - | Endogenous location choice



## 5 THE DECLINE OF THE LABOR SHARE



Decomposition of the decline

$$ds^{v,L} = \frac{\partial s^{v,L}}{\partial \ln w/r} d\ln w/r + \left( ds^{v,L} - \frac{\partial s^{v,L}}{\partial \ln w/r} d\ln w/r \right)$$

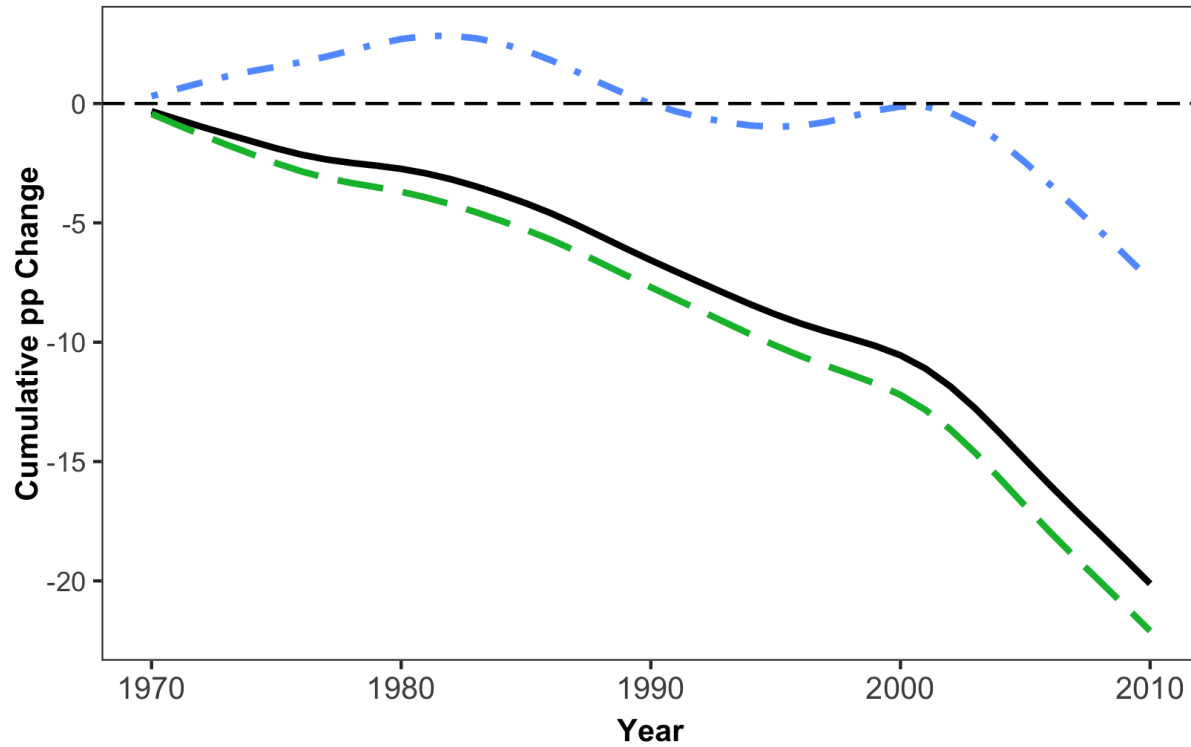
Wage

Tech

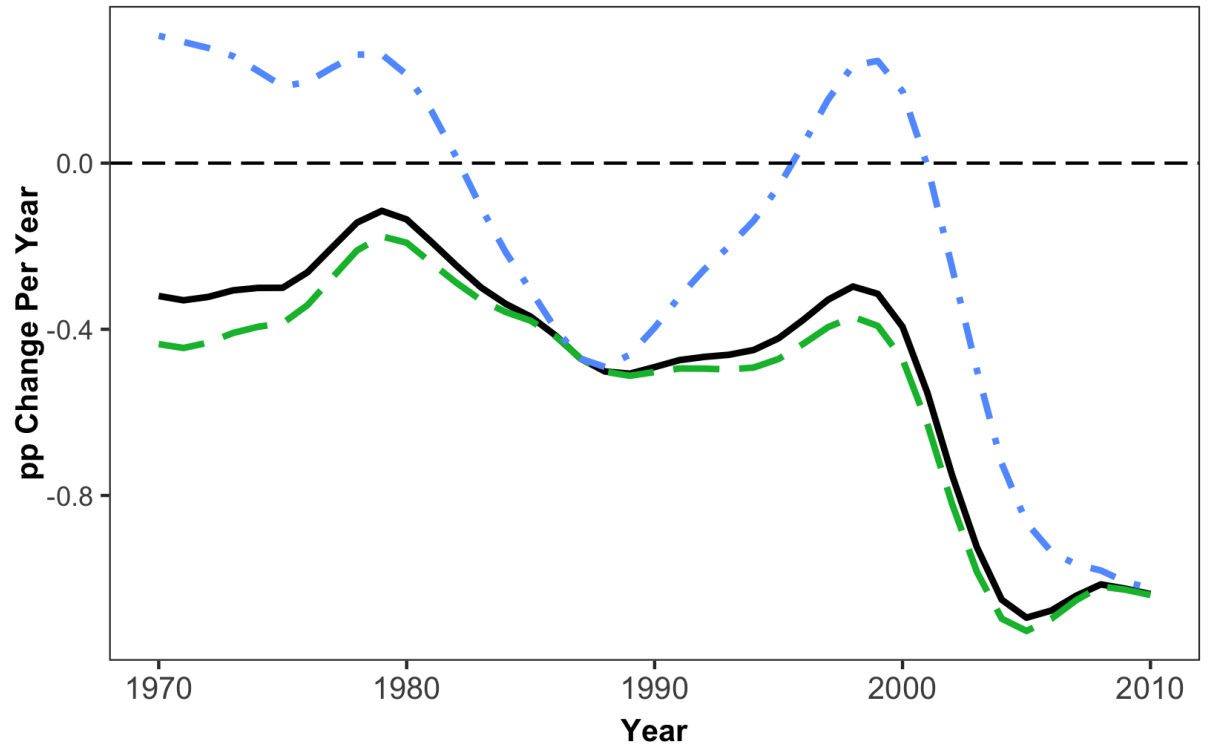


# 5 THE DECLINE OF THE LABOR SHARE

Technical change impacts the labor share



— Baseline    - - - Plant Elasticity    - . - . - Aggregate Elasc = 2



— Baseline    - - - Plant Elasticity    - . - . - Aggregate Elasc = 2



# Micro Data Macro Technology



# THANK YOU



易诗凯  
洪伟励  
邹洛昊  
曾子昂  
孙菁桐

